

Statistical analysis of the determinations of the Sun's Galactocentric distance

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Abstract. Based on several tens of R_0 measurements made during the past two decades, several studies have been performed to derive the best estimate of R_0 . Some used just simple averaging to derive a result, whereas others provided comprehensive analyses of possible errors in published results. In either case, detailed statistical analyses of data used were not performed. However, a computation of the best estimates of the Galactic rotation constants is not only an astronomical but also a metrological task. Here we perform an analysis of 53 R_0 measurements (published in the past 20 years) to assess the consistency of the data. Our analysis shows that they are internally consistent. It is also shown that any trend in the R_0 estimates from the last 20 years is statistically negligible, which renders the presence of a bandwagon effect doubtful. On the other hand, the formal errors in the published R_0 estimates improve significantly with time.

Keywords. Galaxy: center, Galaxy: fundamental parameters

1. Introduction

Accurate knowledge of the distance from the Sun to the center of the Galaxy, R_0 , is important in many fields of astronomy and space science. In particular, the primary motivation for this study was a wish to improve the accuracy of modeling the Galactic aberration (Malkin 2011).

Over the past decades, many tens of R_0 determinations have been made, making use of different principles and observing methods, and thus characterized by different random and systematic errors. Therefore, deriving a best R_0 estimate from these data is not only an astronomical but also a metrological task, similar to deriving the best estimates of the fundamental constants in physics. For the latter, several statistical methods have been developed to obtain best estimates—as well as their realistic uncertainties—from heterogeneous measurements. In this study, we applied those methods to the R_0 data.

Another goal of this study was to investigate a possible trend in the multi-year series of R_0 estimates, as discussed by many authors. However, estimates of any such trend differ significantly among papers. Therefore, we tried to clarify this issue using the latest results. More details are provided by Malkin (2012).

2. Data used

For the present study, we used all R_0 measurements published in the period 1992–2011, with the exception of a number of results that were revised in subsequent papers. We did not use the results of Glushkova *et al.* (1998; revised by Glushkova *et al.* 1999), Paczynski & Stanek (1998; revised by Stanek *et al.* 2000), Eisenhauer *et al.* (2003; revised by Eisenhauer *et al.* 2005, which was in turn revised by Gillessen *et al.* 2009). In total, 53 estimates (listed in Table 1) were used.

Table 1. R_0 estimates used in this study.

R_0 (kpc)	$\pm(1\sigma)$	Reference
7.9	0.8	Merrifield, M.R. 1992, <i>AJ</i> , 103, 1552
8.1	1.1	Gwinn, C.R., <i>et al.</i> 1992, <i>ApJ</i> , 393, 149
7.6	0.6	Moran, J.M., <i>et al.</i> 1993, <i>Lect. Notes Phys.</i> , 412, 244
7.6	0.4	Maciel, W.J. 1993, <i>Ap&SS</i> , 206, 285
8.09	0.3	Pont, F., <i>et al.</i> 1994, <i>A&A</i> , 285, 415
7.5	1.0	Nikiforov, I.I., & Petrovskaya, I.V. 1994, <i>Astron. Rep.</i> , 38, 642
7.0	0.5	Rastorguev, A.S., <i>et al.</i> 1994, <i>Astron. Lett.</i> , 20, 591
8.8	0.5	Glass, I.S., <i>et al.</i> 1995, <i>MNRAS</i> , 273, 383
7.1	0.5	Dambis, A.K., <i>et al.</i> 1995, <i>Astron. Lett.</i> , 21, 291
8.3	1.0	Carney, B.W., <i>et al.</i> 1995, <i>AJ</i> , 110, 1674
8.21	0.98	Huterer, D., <i>et al.</i> 1995, <i>AJ</i> , 110, 2705
7.95	0.4	Layden, A.C., <i>et al.</i> 1996, <i>AJ</i> , 112, 2110
7.55	0.7	Honma, M., & Sofue, Y. 1996, <i>PASJ</i> , 48, L103
8.1	0.4	Feast, M.W. 1997, <i>MNRAS</i> , 284, 761
8.5	0.5	Feast, M., & Whitelock, P. 1997, <i>MNRAS</i> , 291, 683
7.66	0.54	Metzger, M.R., <i>et al.</i> 1998, <i>AJ</i> , 115, 635
8.1	0.15	Udalski, A. 1998, <i>Acta Astron.</i> , 48, 113
7.1	0.4	Olling, R.P., & Merrifield, M.R. 1998, <i>MNRAS</i> , 297, 943
8.51	0.29	Feast, M., <i>et al.</i> 1998, <i>MNRAS</i> , 298, L43
8.2	0.21	Stanek, K.Z., & Garnavich, P.M. 1998, <i>ApJ</i> , 503, L131
8.6	1.0	Surdin, V.G. 1999, <i>Astron. Astrophys. Trans.</i> , 18, 367
7.4	0.3	Glushkova, E.V., <i>et al.</i> 1999, <i>Astron. Astrophys. Trans.</i> , 18, 349
7.9	0.3	McNamara, D.H. <i>et al.</i> 2000, <i>PASP</i> , 112, 202
8.67	0.4	Stanek, K.Z., <i>et al.</i> 2000, <i>Acta Astron.</i> , 50, 191
8.2	0.7	Nikiforov, I.I. 2000, <i>Astron. Soc. Pac. Conf. Ser.</i> , 209, 403
8.24	0.42	Alves, D.R. 2000, <i>ApJ</i> , 539, 732
8.05	0.6	Genzel, R., <i>et al.</i> 2000, <i>MNRAS</i> , 317, 348
8.3	0.3	Gerasimenko, T.P. 2004, <i>Astron. Rep.</i> , 48, 103
7.7	0.15	Babusiaux, C., & Gilmore, G. 2005, <i>MNRAS</i> , 358, 1309
8.01	0.44	Avedisova, V.S. 2005, <i>Astron. Rep.</i> , 49, 435
8.7	0.6	Groenewegen, M.A.T., & Blommaert, J.A.D.L. 2005, <i>A&A</i> , 443, 143
7.2	0.3	Bica, E., <i>et al.</i> 2006, <i>A&A</i> , 450, 105
7.52	0.36	Nishiyama, S., <i>et al.</i> 2006, <i>ApJ</i> , 647, 1093
8.1	0.7	Shen, M., Zhu, Z. 2007, <i>Chin. J. Astron. Astrophys.</i> , 7, 120
7.4	0.3	Bobylev, V.V., <i>et al.</i> 2007, <i>Astron. Lett.</i> , 33, 720
7.94	0.45	Groenewegen, M.A.T., <i>et al.</i> 2008, <i>A&A</i> , 481, 441
8.07	0.35	Trippe, S., <i>et al.</i> 2008, <i>A&A</i> , 492, 419
8.16	0.5	Ghez, A.M., <i>et al.</i> 2008, <i>ApJ</i> , 689, 1044
8.33	0.35	Gillessen, S., <i>et al.</i> 2009, <i>ApJ</i> , 692, 1075
8.7	0.5	Vanhollebeke, E., 2009, <i>A&A</i> , 498, 95
7.58	0.40	Dambis, A.K. 2009, <i>MNRAS</i> , 396, 553
7.2	0.3	Bonatto, C., <i>et al.</i> 2009, <i>Globular Clusters: Guides to Galaxies</i> , p. 209
8.4	0.6	Reid, M.J., <i>et al.</i> 2009, <i>ApJ</i> , 700, 137
7.75	0.5	Majaess, D.J., <i>et al.</i> 2009, <i>MNRAS</i> , 398, 263
7.9	0.75	Reid, M.J., <i>et al.</i> 2009, <i>ApJ</i> , 705, 1548
8.24	0.43	Matsunaga, N., <i>et al.</i> 2009, <i>MNRAS</i> , 399, 1709
8.28	0.33	Gillessen, S., 2009, <i>ApJ</i> , 707, L114
7.7	0.4	Dambis, A.K. 2010, <i>Variable Stars, the Galactic halo and Galaxy Formation</i> , p. 177
8.1	0.6	Majaess, D. 2010, <i>Acta Astron.</i> , 60, 55
8.3	1.1	Sato, M., <i>et al.</i> 2010, <i>ApJ</i> , 720, 1055
7.80	0.26	Ando, K., <i>et al.</i> 2011, <i>PASJ</i> , 63, 45
8.3	0.23	Brunthaler, A., <i>et al.</i> 2011, <i>Astron. Nachr.</i> , 332, 461
8.29	0.16	McMillan, P.J. 2011, <i>MNRAS</i> , 414, 2446

Where both random (statistical) and systematic uncertainties were given, they were summed in quadrature. If two different values were given for the lower and upper boundaries of the confidence interval, the mean value of these boundaries was used as the uncertainty in the result (the lower and upper boundaries were close to each other in all cases, so that this approximation procedure does not significantly affect the final result). Where authors gave several estimates of R_0 without a final preference, the unweighted average of these estimates was computed.

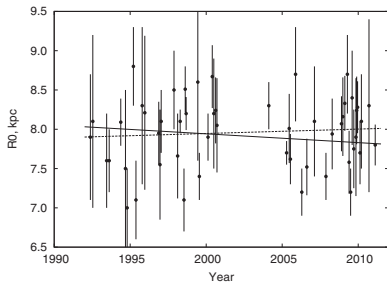


Figure 1. R_0 estimates used in this study. The weighted (solid line) and unweighted (dashed line) trends are also shown.

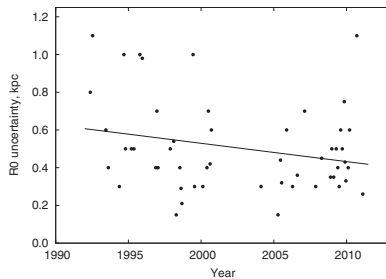


Figure 2. Uncertainty in R_0 estimates used in this study.

3. Results

Our analysis used two approaches. First, we investigated a possible drift in the R_0 values (see Fig. 1), which may indicate the presence of a bandwagon effect. We obtained a linear slope in R_0 as a function of time of $+0.003 \pm 0.010$ kpc yr $^{-1}$ for the weighted case and $+0.009 \pm 0.010$ kpc yr $^{-1}$ for the unweighted case. Thus, any trend in R_0 estimates published in the last 20 years is statistically insignificant, which renders a significant bandwagon effect doubtful. This conclusion is confirmed by application of the Abbe criterion (Malkin 2013). The latter paper also contains a detailed discussion on this subject.

On the other hand, the trend in the reported R_0 uncertainties (see Fig. 2) is statistically significant, i.e., -0.0103 ± 0.0053 kpc yr $^{-1}$. This is particularly interesting because we expect that there are two tendencies in the changes in the errors in R_0 measurements with time. First, the errors should decrease with progress in observational and analysis methods. On the other hand, one can expect that the published errors should increase because most authors of recent papers now pay more attention to the correct computation of the uncertainties in their result. Evidently, the former tendency prevails.

To assess the internal consistency of the R_0 measurements, several statistical methods were used. They can be divided into two groups. The first group consists of computation of the unweighted and classical weighted means, the author's modification with respect to computation of the mean uncertainty (Malkin 2001), and three other weighted-mean modifications, which allow to account for input data discrepancies, i.e., limitation of relative weights (Nichols 2004), normalized residuals (James *et al.* 1992), and the Mandel–Paule method (Paule & Mandel 1982). If all variants of the weighted mean produce the same mean value and standard error, the input data are consistent. The second group of methods includes determination of the median with error estimation (Müller 1995) and bootstrap median methods. Detailed descriptions of these methods are given in Malkin (2012). The results of the computations are presented in Table 2.

4. Concluding remarks

Although the published R_0 estimates were obtained based on different methods and samples of objects, they are consistent rather than discrepant. The results of the computation of a mean R_0 value obtained using different statistical techniques converge at the level of approximately 0.1 kpc, which is much smaller than the uncertainty in the average value. Note, however, that this conclusion is not evident. Similar analysis of Ω_0 measurements has shown that the latter are much less consistent.

Table 2. Average estimates of R_0 obtained with different statistical techniques (see text).

Method	R_0 , kpc
Unweighted mean	7.979 ± 0.061
Classical weighted mean	7.967 ± 0.048
Modified weighted mean	7.967 ± 0.073
Limitation of relative weights	7.967 ± 0.048
Normalized residuals	7.967 ± 0.048
Mandel–Paule method	7.958 ± 0.058
Median	8.090 ± 0.062
Bootstrap median	8.060 ± 0.072

As significant experience in deriving best estimates of the physical constants has shown, using various statistical methods to evaluate the best R_0 estimate is very important to assess data consistency and obtain a realistic uncertainty in the final result. Therefore, careful astronomical consideration of the published measurements should be accompanied by a careful statistical analysis. It should be recognized that the computation of the new conventional IAU R_0 value is not only an astronomical, but also a metrological task.

Another result of this study is that any trend in the R_0 estimates obtained during the last 20 years is statistically insignificant, which makes it unlikely that R_0 results are significantly affected by a bandwagon effect. On the other hand, the formal errors in the published R_0 estimates improve significantly with time.

Note that the average value $R_0 = 8.0 \pm 0.25$ kpc computed in this study differs from the results of the latest direct measurements obtained from stellar orbits about Sgr A*, trigonometric parallaxes to Sgr B2, and over 60 trigonometric parallaxes of masers, which give $R_0 = 8.4 \pm 0.2$ kpc (M. J. Reid, priv. comm.), although these values are still statistically consistent.

On the other hand, it seems important to properly combine all results obtained based on different methods, because this provides better systematic stability of the average result. Indeed, the systematic and random errors of all these results should be assessed and the corresponding correction should be applied when possible before averaging (although this is a very difficult task).

References

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